

## Remember your trig formulas

Pythagorean identities:

$$\sin^2 x + \cos^2 x = 1$$

$$\tan^2 x + 1 = \sec^2 x$$

$$1 + \cot^2 x = \csc^2 x$$

Sum and difference formulas:

$$\sin(a \pm b) = \sin a \cos b \pm \cos a \sin b$$

$$\cos(a \pm b) = \cos a \cos b \mp \sin a \sin b$$

$$\tan(a \pm b) = \frac{\tan a \pm \tan b}{1 \mp \tan a \tan b}$$

Double angle formulas:

$$\sin(2a) = 2 \sin a \cos a$$

$$\cos(2a) = \cos^2 a - \sin^2 a$$

$$= 2 \cos^2 a - 1$$

$$= 1 - 2 \sin^2 a$$

$$\tan(2a) = \frac{2 \tan a}{1 - \tan^2 a}$$

Half angle formulas:

$$\sin\left(\frac{a}{2}\right) = \pm \sqrt{\frac{1 - \cos(a)}{2}}$$

$$\cos\left(\frac{a}{2}\right) = \pm \sqrt{\frac{1 + \cos(a)}{2}}$$

$$\tan\left(\frac{a}{2}\right) = \pm \sqrt{\frac{1 - \cos a}{1 + \cos a}}$$

Domains and Ranges of Trig Functions:

$$f(x) = \sin x$$

Domain: All real numbers

Range:  $[-1, 1]$

$$f(x) = \cos x$$

Domain: All real numbers

Range:  $[-1, 1]$

$$f(x) = \tan x$$

Domain:  $x \neq k\frac{\pi}{2}, k$  any integer

Range: All real numbers

$$f(x) = \csc x$$

Domain:  $x \neq k\pi, k$  any integer

Range:  $(-\infty, -1] \cup [1, \infty)$

$$f(x) = \sec x$$

Domain:  $x \neq k\frac{\pi}{2}, k$  any integer

Range:  $(-\infty, -1] \cup [1, \infty)$

$$f(x) = \cot x$$

Domain:  $x \neq k\pi, k$  any integer

Range: All real numbers

Principal Inverse trig functions:

$$\text{Arcsin}(x)$$

Domain:  $[-1, 1]$

Range:  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$  (first and fourth quadrants)

$$\text{Arccos}(x)$$

Domain:  $[-1, 1]$

Range:  $[0, \pi]$  (first and second quadrants)

$$\text{Arctan}(x)$$

Domain: All real numbers

Range:  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$  (first and fourth quadrants)

The other three inverse functions were purposefully omitted.

General info on arcs and sectors of circles:

Length of an arc of a circle intercepted by an angle  $a$ :  $L = \frac{a}{2\pi} \cdot 2\pi r = ar$

Area of a sector of a circle intercepted by an angle  $a$ :  $A = \frac{a}{2\pi} \pi r^2 = \frac{ar^2}{2}$